

DO NOT TURN TO THE NEXT PAGE until your proctor tells you.

Please read the directions carefully.

- ▶ You have 100 minutes for 32 Problems.
- ▶ Mark your answers on your Answer Form with a pencil.
- ▶ Extra scratch paper is neither given nor allowed. You may use blank pages/spaces in the booklet as scratch paper.
- ▶ There are no penalties for incorrect answers. Answer as many problems as you can; go back and check your work and also go to questions you skip, before the time is over.

- ▶  Use of calculators is prohibited. Cell phones must be turned off completely and placed out of sight. MathCON problems are ALL done without a calculator.

- ▶ The problems are divided into three categories by the difficulty levels:
3 Points (Questions 1-8)
5 Points (Questions 9-24)
7 Points (Questions 25-32)

- ▶ Problems 29-32, the last four problems are constructed-response problems. Enter your numerical answer in the grid on your answer sheet as shown on the right.

1. Although not required, it is suggested that you write your answer from left to right in the boxes at the top of the columns to help you fill in the circles accurately. You will receive credit only if the circles are filled in correctly.

2. Mark no more than one circle in any column.
3. You may start your answers in any column, space permitting. Leave unused columns blank, and there should be no blank columns between columns that are not blank. For example, if your answer is 201, then either arrangement of filled-in circles shown below is acceptable.

For example: Answer: 201 – either position is correct.

	2	0	1
Ⓐ	Ⓐ	●	Ⓐ
Ⓑ	Ⓑ	Ⓑ	●
Ⓒ	●	Ⓒ	Ⓒ
Ⓓ	Ⓓ	Ⓓ	Ⓓ

2	0	1	
Ⓐ	●	Ⓐ	Ⓐ
Ⓑ	Ⓑ	●	Ⓑ
●	Ⓒ	Ⓒ	Ⓒ
Ⓓ	Ⓓ	Ⓓ	Ⓓ

4. No problem has a negative answer.

▶ Notations in Geometry Problems:

- A : Point A
- $\overleftrightarrow{AB}$: Line through points A and B
- $\overline{AB}$: Line segment joining A and B
- AB : Length of the line segment AB
- $\angle ABC$: Angle with the vertex point at B
- $m\angle ABC$: Measure of angle ABC
- $\perp$: Perpendicular
- // : Parallel

1. [Algebra, 3 Points]

What is the value of the following product?

$$\log_{100}2 \times \log_23 \times \log_34 \times \log_45 \times \dots \times \log_{99}100$$

- A) 1 B) $\log_2100$ C) $\log_{100}2$ D) $\log_2100 + \log_{100}2$ E) 100

4. [Combinatorics, 3 Points]

Six balls are labeled with consecutive integers 1, 2, 3, 4, 5, and 6.

Two of the balls are chosen at random.

What is the probability that the two chosen balls have consecutive numbers?

- A) $\frac{1}{3}$ B) $\frac{5}{12}$ C) $\frac{1}{2}$ D) $\frac{7}{12}$ E) None of the preceding

5. [Algebra, 3 Points]

If positive real number k is the solution of the below equation

$$3x^2 + kx - 2 = 0$$

which of the following is the other solution?

- A) $\frac{\sqrt{2}}{3}$ B) $\frac{2\sqrt{2}}{3}$ C) $-\frac{2\sqrt{2}}{3}$ D) $\frac{\sqrt{2}}{6}$ E) $-\frac{\sqrt{3}}{6}$

7. [Number Theory, 3 Points]

Let $D(n)$ be the sum of the digits of the positive integer n .

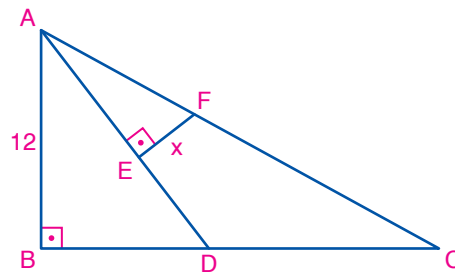
For example, $D(2026) = 10$.

If $D(n) = 1275$, which of the following could be the value of $D(n + 1)$?

- A) 7 B) 8 C) 9 D) 10 E) None of the preceding

10. [Geometry, 5 Points]

In the given figure,
 ABC is a right triangle,
 $AB \perp BC$,
 $FE \perp AD$,
 $AD = DC$,
 $CF = 2 \cdot FA$,
 $AB = 12$ cm, and
 $EF = x$ cm.
 What is the value of x ?



- A) 2 B) 3 C) 4 D) 5 E) 6

11. [Number Theory, 5 Points]

The sum of three different prime numbers is 20.

What is the **least** possible product of these three numbers?

- A) 102 B) 130 C) 138 D) 154 E) 182